

Book-keeping --> accounting --> balance --> state

**Bookkeeping** is the recording of financial transactions, and is part of the process of **accounting** in **business**.<sup>[1]</sup> Transactions include purchases, sales, receipts and payments by an individual person or an organization/corporation. There are several standard methods of bookkeeping, including the **single-entry** and **double-entry** bookkeeping systems.

From <<https://en.wikipedia.org/wiki/Bookkeeping>>  
<https://www.dreamstime.com/stock-image-d-life-cycle-accounting-process-illustration-circular-flow-chart-image30625511>



- Authorized capital
- Credit
- Fixed Assets
- Costs
- Incomes

Op.No. Input Output RemainingAmount

1	123	0	123
2	5	11	117

Compare with UTxO system

<https://medium.com/@olxc/ethereum-and-smart-contracts-basics-e5c84838b19>

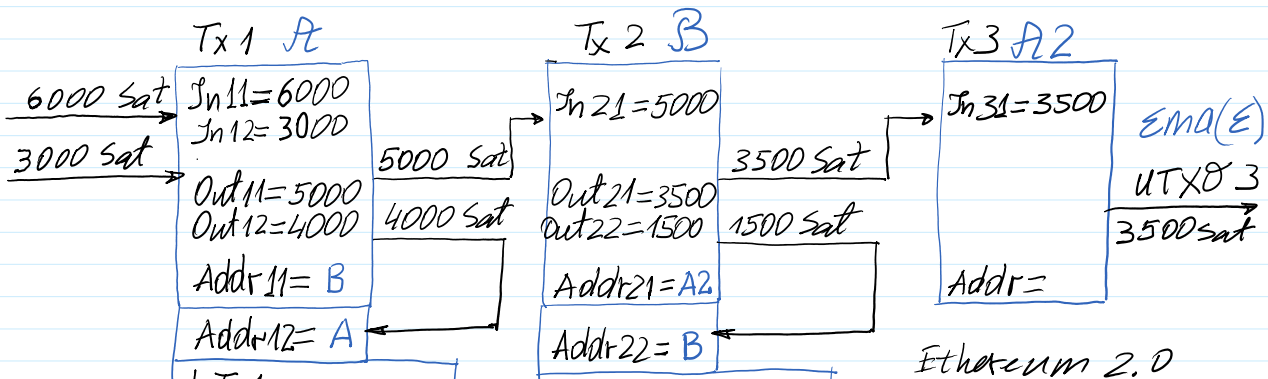
<b>State 0</b>	Authorized Capital	Credit	Fixed Asset				<b>Balance 0</b>
	12 000	9 000	-12 000				<b>9 000</b>

<b>State 1</b>	Authorized Capital	Credit	Electricity Cost 1	Mining 1	Percent for Credit		<b>Balance 1</b>
		9 000	-3 000	+31 000	-1 000		<b>36 000</b>

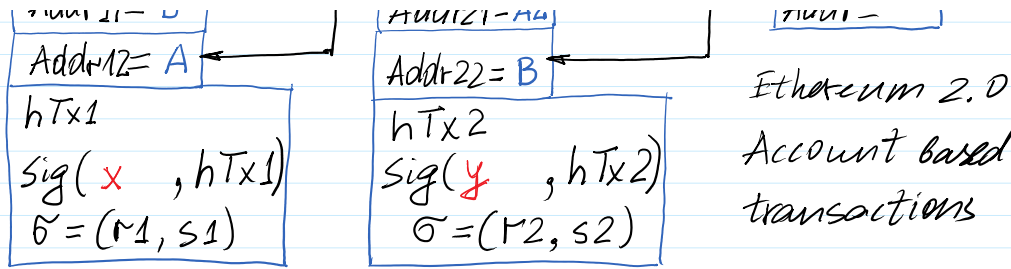
<b>State 2</b>	Authorized Capital	Credit	Electricity Cost 2	Mining 2	Percent for Credit		<b>Balance 2</b>
		8 000	-15 000	-	-1 000		<b>20 000</b>

Book-keeping --> Accounting --> Balance --> State

UTxO system



Ethereum 2.0



Tx1 = '1: In11 = 6000 || In12 = 3000 || Out11 = 5000 || Out12 = 4000 || Rec1 = B || Rec2 = A'  
 Tx2 = '2: In21 = 5000 || Out21 = 3500 || Out22 = 1500 || Rec1 = A2 || Rec2 = B'  
 Tx3 = '3: In31 = 3500 || Out31 = 3500 || Rec = E'

$$h_1 = H(Tx1) = h28(Tx1)$$

$$h_2 = H(Tx2) = h28(Tx2)$$

$$h_3 = H(Tx3) = h28(Tx3)$$

Transaction template:

Tx\_N = 'Tx\_N:In11=... || In12=... || Out11=... || Out12=... || Rec1=... || Rec2=...'

Transactions:

Tx\_1 = 'Tx\_1:In11=6000 || In12=3000 || Out11=5000 || Out12=4000 || Rec1=B || Rec2=A'

Tx\_2 = 'Tx\_2:In21=5000 || Out21=3500 || Out22=1500 || Rec1=A2 || Rec2=B'

Tx\_3 = 'Tx\_3:In31=3500 || Out31=3500 || Out32=0 || Rec1=E || Rec2=A2'

>> hTx\_1=h28('Tx\_1:In11=6000 || In12=3000 || Out11=5000 || Out12=4000 || Rec1=B || Rec2=A')

hTx\_1 = 996BB7C

>> hTx\_1=h28(Tx\_1)

hTx\_1 = 996BB7C

>> hTx\_2=h28('Tx\_2:In21=5000 || Out21=3500 || Out22=1500 || Rec1=A2 || Rec2=B')

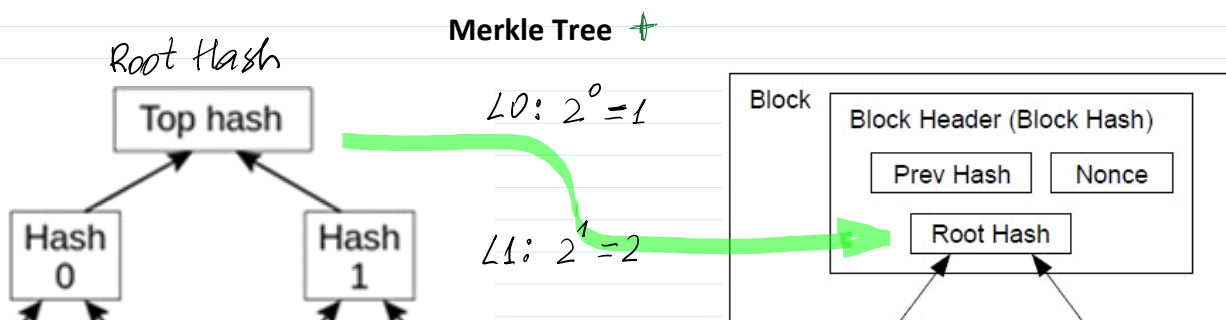
>> hTx\_2=h28(Tx\_2)

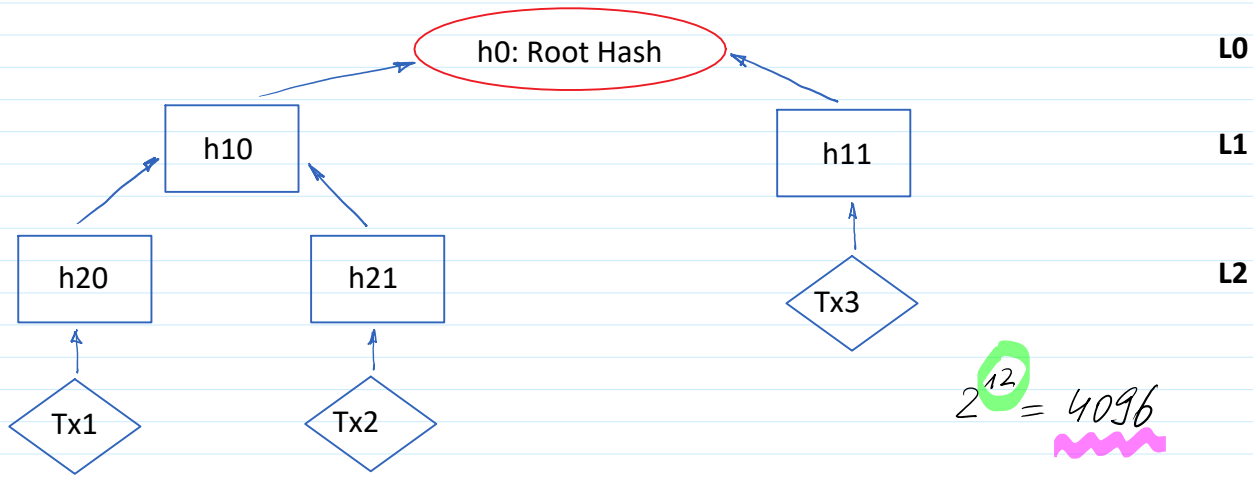
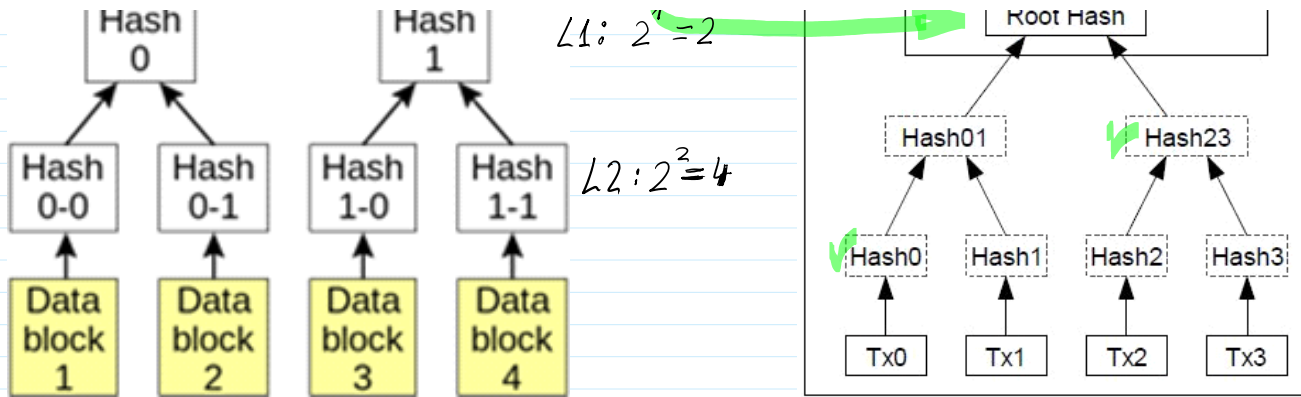
hTx\_2 = 977D75B

>> hTx\_3=h28('Tx\_3:In31=3500 || Out31=3500 || Out32=0 || Rec1=E || Rec2=A2')

>> hTx\_3=h28(Tx\_3)

hTx\_3 = 9201218





```

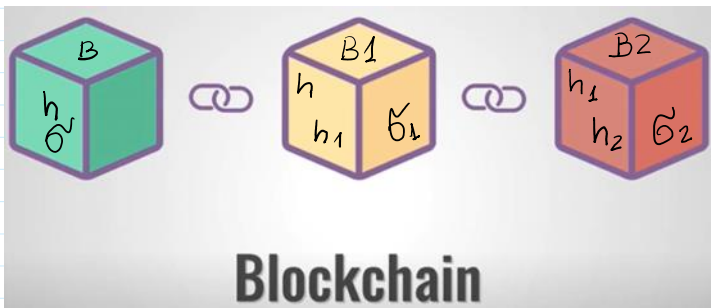
>> h20=h28(hTx_1)
h20 = 996BB7C
>> h21=h28(hTx_2)
h21 = 977D75B
>> h10=h28('996BB7C|977D75B')
h10 = 9201218
>> h11=h28(hTx_3)
h11 = 9201218
>> h0=h28('9201218|9201218')
h0 = 08E7C34

```

**Root Hash: h0**

Python : sha256

h20: 5B5412B                      h10: 625A41F  
h21: D5C895A                      h0: **60BA3B5**  
h11: FEC59B7



Magic Number (4)	Block Size (4)
Version (4)	Previous Block Hash (32)
SHA 256 bits	
Merkle Root(32)	
Timestamp (4)	
Difficulty Target (4)	Nonce (4)
Transaction Counter (Variable : 1-9)	
Transaction List (Variable : Upto 1 MB)	

BLOCK HEADER

Block size = 4 Bytes  
 4 Bytes x 8 bits = 32 bits  
 Block have  
 $2^{32} - 1 = 4294967295$   
 In ASCII encoding  
 8 bits represents  
 1 symbol a, b, c, ...  
 Block represents  
 536 870 912 symbols

Difficulty Target (DT): defines the complexity of block mining.  
 In our simulation DT we will choose to find h-value of mining (mined block) having only 1 leading hexadecimal digit equal to 0.

$$h_{28}(\text{RootHash} \_ \text{PrevHash} \_ 737327631) =$$

```
>> sha256('RootHash PrevHash 737327631')
```

```
ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130ED C51E6DE
```

C51E6DE

```
>> sha256('RootHash PrevHash 737327632')
```

```
ans = B856211DF2EE15E30AB770C1A43CE014ECFE573182AFD885B28D96854DBC5F21
```

```
>> sha256('RootHash PrevHash 737327633')
```

```
ans = 9C18C764E347A58E57AC3F7A3C2874D5889A0E802699FEA47EEFF8C03BFEDA69
```

DT: to mine a block it is needed to find h-value having leading zero in hexadecimal format: C51E6DE 0XXXXXX

F  
1111

↓  
6 × 4 = 24 bits

h-value is computed so  $\gg h_{28}(\ ) \rightarrow 7$  hex numbers

What probability to mine a block?

The number of possible h-values of 28 bits:  $2^{28}$

$\gg 2^{28}$  ans = 268 435 456

The number of adequate h-values:  $2^{24}$

$\gg \text{int64}(2^{24})$  ans = 16777216

$$\Pr\{\text{to Mine}\} = \frac{2^{24}}{2^{28}} = \frac{1}{2^4} = \frac{1}{16}$$

DT: two leading hex number = 00

The number of adequate h-values:  $2^{20}$

00XXXXX

$$\downarrow$$

$$5 \times 4 = 20$$

$$\Pr\{\text{to Mine}\} = \frac{2^{20}}{2^{28}} = \frac{1}{2^8} = \frac{1}{256}$$

DT: two leading hex number = 000

000XXXX

$$4 \times 4 = 16$$

$$\Pr\{\text{to Mine}\} = \frac{2^{16}}{2^{28}} = \frac{1}{2^{12}} = \frac{1}{4096}$$

$$\gg 2^{12} \text{ ans} = 4096$$

$$\Pr\{\text{to Mine}\} = \frac{1}{2^{28}} = \frac{1}{268\,435\,456}$$

$$\gg 2^{28} \text{ ans} = 268\,435\,456$$

The probability to mine a block, e.g. in Bitcoin when

DT: is to find SHA256 value having 18 leading zeroes

>> sha256('RootHash PrevHash 737327631')

ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE  
00000000000000000000 XX

The number of possible h-values having 256 bits is  $2^{256}$ .

The number of adequate h-values of SHA256 is

$$256 - 18 \cdot 4 = 256 - 72 = 184 \text{ bits, that are represented 46 hex. num.}$$

The number of adequate values is  $2^{184}$ .

$$\text{Prob}\{\text{to mine}\} = \frac{2^{184}}{2^{256}} = 2^{184-256} = 2^{-72}$$

$$1 \text{ K} = 2^{10} = 1024$$

$$1 \text{ M} = 2^{20} = \dots$$

$$1 \text{ G} = 2^{30} = \dots$$

$$1 \text{ T} = 2^{40} = \dots$$

$$2^{72} \sim 4 \text{ GT} = 4 \cdot 2^{30} \cdot 2^{40} = 2^2 \cdot 2^{30} \cdot 2^{40} = 2^{72}$$

Private blockchain  $\longleftrightarrow$  Public blockchain

Monero blockchain: Transactions sums  $\rightarrow$  confidential  $\rightarrow$  verifiable  
 Sender }  $\rightarrow$  anonymous  
 Receiver }

How to realize confidential & verifiable transactions.